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Editors of the Volume

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PREFACE

In Autumn of 1992 the International Banach Center in Warsaw organized a Semester on Complex Analysis. The form of this semester was similar to that held at the Banach Center in 1979. It was divided into six blocks, called minisemesters, devoted to the following branches of complex analysis:

1. *Invariant pseudodistances in complex analysis*
   (chairmen: M. Jarnicki and P. Pflug);
2. *Extremal problems of the theory of functions of one complex variable*
   (chairman: J. Krzyż);
3. *Boundary properties of holomorphic functions and mappings including CR-theory*
   (chairmen: E. M. Chirka, A.-M. Chollet and P. Jakóbczak);
4. *$\bar{\partial}$-equation and applications*
   (chairmen: E. M. Chirka, A.-M. Chollet and P. Jakóbczak);
5. *Integral representations and residues*
   (chairmen: L. A. Aizenberg and P. Jakóbczak);
6. *Approximation in complex domain*
   (chairman: W. Pleśniak)

Wiesław Pleśniak also served as chairman of the Organizing Committee.

There were 139 participants from 25 countries and 134 lectures were given by 110 lecturers. The Organizers of the Semester have been encouraged to follow the tradition of the Banach Center Semesters by publishing the Proceedings of this event. This volume contains some papers that were contributed to the Semester. The Editors would like to thank very warmly the authors of the submitted papers for their contribution. Special thanks are addressed to Zbigniew Błocki, Jacques Chaumat, Anne-Marie Chollet and Jan Krzyż for their help in preparing the material for publication in this volume.

Cracow, January 1994

Piotr Jakóbczak and Wiesław Pleśniak
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