

POLISH ACADEMY OF SCIENCES  
INSTITUTE OF MATHEMATICS

**BANACH  
CENTER**  
Publications

VOLUME **28**

Algebraic Methods in  
Logic and in  
Computer Science

WARSZAWA 1993

ALGEBRAIC METHODS  
IN LOGIC AND  
IN COMPUTER SCIENCE

*Editor of the Volume*

CECYLIA RAUSZER

WARSZAWA 1993

Published by the Institute of Mathematics, Polish Academy of Sciences

Typeset in T<sub>E</sub>X at the Institute

Printed and bound by

*drukarnia*  
**herman & herman**

02-240 Warszawa, ul. Jakobińców 23, tel: 846-79-66, tel/fax: 49-89-95

P R I N T E D I N P O L A N D

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ISBN 83-85116-92-3

ISSN 0137-6934

## PREFACE

The XXXVIII Semester on *Algebraic Methods in Logic and their Computer Science Applications*, organized by the Stefan Banach International Mathematical Center, was held in Warsaw between September 15 and December 15, 1991.

It was divided into four sections covering the following topics: *Universal Algebra* (November 1–December 15), *Algebraic Logic* (September 15–October 30), *Algebra and Logic in Computer Science* (September 15–December 15) and *Applications in Physics and in the Theory of Cellular Automata* (November 1–December 15). The organizing committee consisted of H. Andr eka and I. N emeti (both Sec. II), C. Rauszer (Sec. III) and the chairman of the committee, M. M aczyński (Secs. I & IV).

During these three months 118 invited speakers from 25 countries gave around 200 hours of talks. This resulted in a large number of high quality papers being presented to the proceedings of the Semester, which are traditionally published in the Banach Center Publications series. The papers were carefully evaluated, although it was clear that their sheer number was too large for them to be published in a single volume only. Moreover, considering the rich variety of material presented during the Semester, I have decided that a complementary two-volume compilation of the proceedings is more appropriate.

The present volume contains papers from all four sections, although the majority of papers from Section III (*Algebra and Logic in Computer Science*) have already appeared in a special issue of *Fundamenta Informaticae*. Let me take this opportunity to express my gratitude to all the participants for their interest in the Semester, to the authors of all the submitted papers for their valuable contribution, and to all the referees of both volumes. Very special thanks are due to Hajnal Andr eka and Istv an N emeti for their invaluable work during the Semester and for their help in the preparation of the proceedings.

Warszawa, February 1993

*Cecylia Rauszer*

## CONTENTS

Preface . . . . .	5
C. BRINK, From two- to four-valued logic . . . . .	9–16
J. M. FONT, On the Leibniz congruences . . . . .	17–36
J. O. M. JASPARS, Normal forms in partial modal logic . . . . .	37–50
D. PIGOZZI and A. SALIBRA, Polyadic algebras over nonclassical logics . . . . .	51–66
A. SALIBRA and G. SCOLLO, Compactness and Löwenheim–Skolem properties in categories of pre-institutions . . . . .	67–94
A. SIMON, What the finitization problem is not . . . . .	95–116
S. D. COMER, On connections between information systems, rough sets and algebraic logic . . . . .	117–124
I. KOREC, Generalized Pascal triangles: overview of new results . . . . .	125–134
Z. PAWLAK and A. SKOWRON, Rough membership functions: a tool for reasoning with uncertainty . . . . .	135–150
D. SKORDEV, On the detection of some periodic loops during the execution of Prolog programs . . . . .	151–166
R. BERGHAMMER and G. SCHMIDT, Relational specifications . . . . .	167–190
D. A. BREDIKHIN, On algebras of relations . . . . .	191–199
R. D. MADDUX, Finitary axiomatizations of the true relational equations . . . . .	201–208
S. MIKULÁS, Strong completeness of the Lambek Calculus with respect to Relational Semantics . . . . .	209–217
W. J. BLOK and I. M. A. FERREIRIM, Hoops and their implicational reducts (abstract) . . . . .	219–230
I. DÜNTSCH, A note on cylindric lattices . . . . .	231–238
P. JIPSEN, Discriminator varieties of Boolean algebras with residuated operators . . . . .	239–252
J. D. MONK, Lectures on cylindric set algebras . . . . .	253–290
H. A. PRIESTLEY, Natural dualities for varieties of distributive lattices with a quantifier . . . . .	291–310
I. SAIN, Weak products of universal algebras . . . . .	311–318
J. SMITH, Comtrans algebras and their physical applications . . . . .	319–326
R. J. THOMPSON, Complete description of substitutions in cylindric algebras and other algebraic logics . . . . .	327–342